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# B.M.S COLLEGE FOR WOMEN, AUTONOMOUS BENGALURU - 560004 <br> SEMESTER END EXAMINATION - MARCH/APRIL- 2023 

B.Sc. in Mathematics - III Semester

## REAL ANALYSIS- I AND ORDINARY DIFFERENTIAL EQUATIONS (NEP Scheme 2021-22 onwards)

## Instructions: Answer all the sections.

I. Answer any SIX Questions.
( $6 \times 2=12$ )

1. Define bounded sequence
2. Find the limit of the sequence $\frac{3 n-3}{4 n+3}$
3. Test the convergence of the series $\frac{1}{1.3}+\frac{2}{3.5}+\frac{3}{5.7}+\ldots . . \infty$
4. State Raabes's test for convergence
5. Show that the equation $\left(x^{2}-a y\right) d x+\left(y^{2}-a x\right) d y=0$ is exact
6. Solve $\frac{d y}{d x}+2 x y=2 e^{-x}$
7. Find the particular integral of $\left(D^{2}-4 D+3\right) y=e^{x}$
8. Solve $\left(D^{2}-7 D+6\right) y=0$

## II. Answer any FOUR Questions.

1. Prove that every convergent sequence is bounded. Is the converse true. Justify your Answer.
2. Discuss the behaviour of the sequence $\left\{n^{1 / n}\right\}$
3. Show that the sequence $\left\{x_{n}\right\}$ defined by $x_{1}=\sqrt{7}, \quad x_{n+1}=\sqrt{7+x_{n}}$ converges to the positive root of $x^{2}-x-7=0$
4. State Cauchy's root for a series of positive terms.
5. Discuss the convergence of the series $\frac{2}{3}+\frac{2.4}{3.5}+\frac{2.4 .6}{3.5 .7}+\ldots \infty$
6. Sum to infinity $1+\frac{1+2}{2!}+\frac{1+2+2^{2}}{3!}+\ldots$.
1.Solve $p^{2}+2 p y \cot x-y^{2}=0$
7. Solve $\frac{d y}{d x}+\frac{3 x^{2}}{1+x^{3}} y=\frac{\sin ^{2} x}{1+x^{3}}$
8. Find the orthogonal trajectories of family of parabolas $y^{2}=4 a x$
9. Solve $\left(D^{2}+2 D+1\right) y=2 e^{2 x}$
10. Solve the simultaneous equations $\frac{d x}{d t}+7 x-y=0 \& \frac{d y}{d t}+2 x+5 y=0$
11. Solve $\frac{d^{2} y}{d x^{2}}-y=\frac{2}{1+e^{x}}$ by the method of variation of parameters
